

# PLANNING

Sebastian Ordyniak



# Introduction

## Planning:

- ▶ central problem in AI,
- ▶ general framework that concerns the realization of strategies or action sequences, typically for execution by intelligent agents,
- ▶ many variants of different difficulty considered.



## Example: Towers of Hanoi

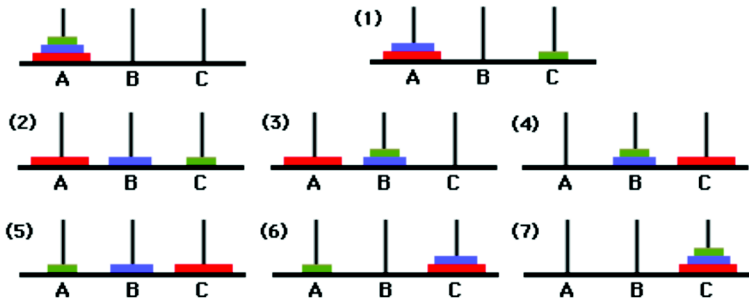


**Initial State**



**Goal State**

# Example: Towers of Hanoi



Solution = Plan

# Classical Planning

## Planning Instance

- ▶ set of **variables** together with their **domains**
- ▶ set of **actions**, each actions has:
  - ▶ a **precondition** and
  - ▶ an **effect**

both precondition and effect are a partial assignment of the variables

- ▶ an **initial state** (a complete assignment of the variables)
- ▶ a **goal state** (a partial assignment of the variables)

# Planning: Problems

## PLANNING

**Input:** A planning instance  $P$ .

**Question:** Compute a plan for  $P$  or output that no plan for  $P$  exists.

## OPTIMAL PLANNING

**Input:** A planning instance  $P$ .

**Question:** Compute a plan of minimum length for  $P$  or output that no plan for  $P$  exists.

## BOUNDED PLANNING

**Parameter:**  $k$

**Input:** A planning instance  $P$  and a natural number  $k$ .

**Question:** Is there a plan for  $P$  of length at most  $k$ ?

# Classical Complexity

- ▶ Classical Planning is **PSPACE**-complete in general.
- ▶ However, various natural restrictions are known under which planning becomes (non-deterministic) polynomial-time tractable, e.g.:
  - ▶ syntactical restrictions (P,U,B,S)
  - ▶ restrictions on the number of preconditions and effects
  - ▶ structural restrictions on the causal graph;

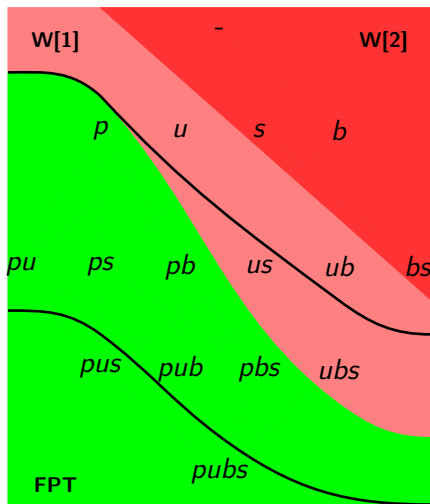


# BOUNDED PLANNING parameterized by “plan length”

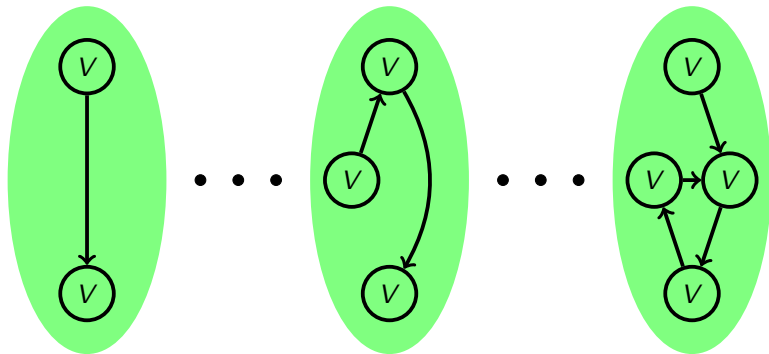
	$m_e = 1$	fix $m_e > 1$	arb. $m_e$
$m_p = 0$	in P in P	in W[1] NP-C	W[2]-C NP-C
$m_p = 1$	W[1]-C NP-H	W[1]-C NP-H	W[2]-C PSPACE-C
fix $m_p > 1$	W[1]-C NP-H	W[1]-C PSPACE	W[2]-C PSPACE
arb. $m_p$	W[1]-C PSPACE-C	W[1]-C PSPACE-C	W[2]-C PSPACE-C

**Bylander's restrictions**

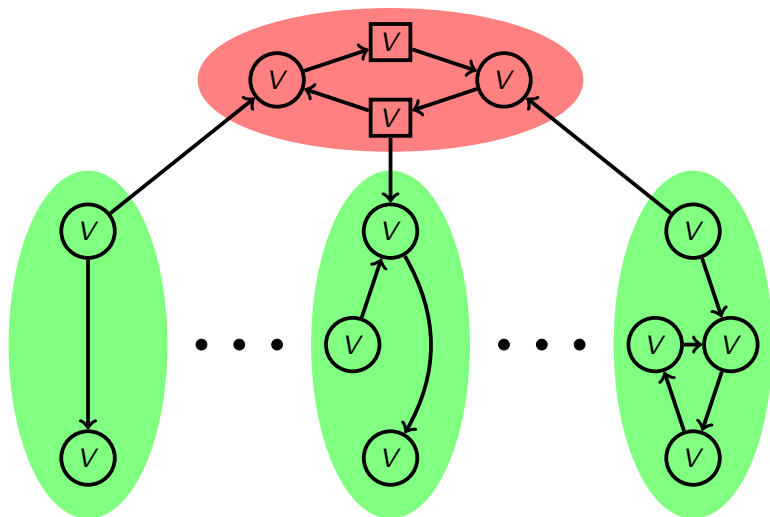
# BOUNDED PLANNING parameterized by “plan length”



# Almost Independent Planning Instances

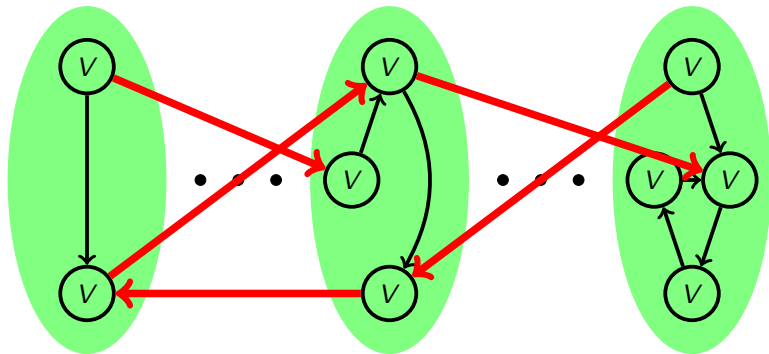


# Almost Independent Planning Instances



Few “global variables”

# Almost Independent Planning Instances



Few “global actions”

# Almost Independent Planning Instances

## Theorem

Bounded domain planning is fixed-parameter tractable parameterized by the number of global actions.

## Theorem

Bounded domain planning is fixed-parameter tractable parameterized by the number of global variables.<sup>1</sup>

We also obtain matching hardness results for all the other combinations.

---

<sup>1</sup>We are still working on a constructive version of this algorithm :) 

**Thank You!**